

**MATH 125 (INTERMEDIATE ALGEBRA)SAMPLE FINAL EXAM**

**INSTRUCTOR: ANNE SISWANTO; TOTAL POINTS: 200; TIME: 120 MINUTES.**

Direction: Please write your answer in the answer blanks and show all work to get full credits. No graphing calculator can be used.

**(5 POINTS) Solve and graph. Write the solution in interval notation.**

1)  $4x - 2 < -22$  and  $6 - 5x > 26$

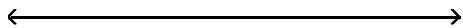
1) \_\_\_\_\_



**(6 POINTS) Solve and graph. Write the solution in interval notation.**

2)  $4 - |4 - 4x| > -3$

2) \_\_\_\_\_



3)  $2|z + 2| + 2 \geq 15$

3) \_\_\_\_\_



**(4 POINTS) Solve the system of equations using substitution.**

4)

$$\begin{cases} x - 4y = -24 \\ -7x - 5y = 3 \end{cases}$$

4) \_\_\_\_\_

**(4 POINTS) Solve the system of equations using the elimination method.**

5)

$$\begin{cases} 8x + 4y = -20 \\ -5x + 2y = -10 \end{cases}$$

5) \_\_\_\_\_

**(8 POINTS) Solve using Cramer's Rule or substitution.**

6)

$$\begin{cases} x - y + 3z = 19 \\ 2x + z = 5 \\ x + 3y + z = -7 \end{cases}$$

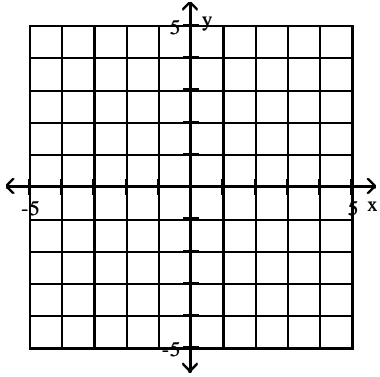
6) \_\_\_\_\_

(6 POINTS) Graph the solution of the system. Label at least two points on each line.

7)

$$\begin{cases} x + 2y \geq 2 \\ x - y \leq 0 \end{cases}$$

7) \_\_\_\_\_



(3 POINTS) Simplify the radicals and then find the sum or difference.

8)  $-10\sqrt{72} + 7\sqrt{200} + 4\sqrt{98}$

8) \_\_\_\_\_

(3 POINTS) Multiply using FOIL.

9)  $(3\sqrt{3} + 4\sqrt{17})(4\sqrt{2} + 3\sqrt{5})$

9) \_\_\_\_\_

(3 POINTS) Rationalize the denominator and simplify.

10)  $\frac{15}{\sqrt{13}}$

10) \_\_\_\_\_

(4 POINTS) Rationalize the denominator and simplify.

11)  $\frac{\sqrt{7}}{7\sqrt{6} - \sqrt{7}}$

11) \_\_\_\_\_

**(3 POINTS) Multiply.**

12)  $(2 - 8i)(6 + 6i)$

12) \_\_\_\_\_

**(4 POINTS) Write the quotient in standard form.**

13)  $\frac{8 + 2i}{3 - 7i}$

13) \_\_\_\_\_

**(5 POINTS) Solve.**

14)  $(2m - 1)^2 = -9$

14) \_\_\_\_\_

**(7 POINTS) Solve the equation by completing the square.**

15)  $p^2 + 3p - 9 = 0$

15) \_\_\_\_\_

16)  $x^2 - 10x + 61 = 0$

16) \_\_\_\_\_

**(7 POINTS) Solve using the quadratic formula.**

17)  $8x^2 + 7x = -2$

17) \_\_\_\_\_

**(7 POINTS) Solve the equation and state the solutions.**

18)  $\frac{16}{x+2} = 1 + \frac{2}{x-4}$

18) \_\_\_\_\_

19)  $\sqrt{x+7} + 5 = x$

19) \_\_\_\_\_

(7 POINTS) Solve.

20)  $x^4 - 3x^2 - 4 = 0$

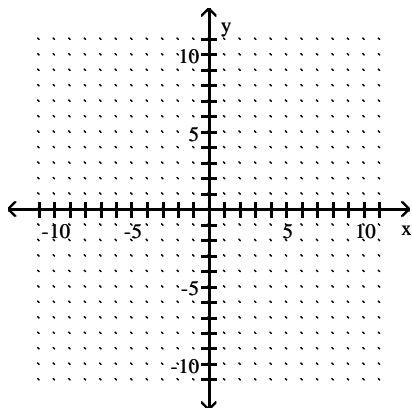
20) \_\_\_\_\_

(8 POINTS)

- a. State whether the graph opens up or down
- b. Find the coordinate of the vertex
- c. Find the equation of the axis of symmetry
- d. Use additional points, graph, and label at least 5 points.

21)  $g(x) = -x^2 + 2x + 1$

21) \_\_\_\_\_



(6 POINTS) Solve the inequality, graph the solution set, and write the solution using interval notation.

22)  $x^2 + 2x < 3$

22) \_\_\_\_\_



**(8 POINTS) Solve the inequality, graph the solution set, and write the solution using interval notation.**

23)  $\frac{3x}{-5x + 17} \geq 3$

23) \_\_\_\_\_



**(5 POINTS) Find the indicated composition.**

24)  $f(x) = 2\sqrt{x + 9}$ ;  $g(x) = 5x + 7$   
Find  $(f \circ g)(x)$ .

24) \_\_\_\_\_

**(5 POINTS) Find  $f^{-1}(x)$  for the following one-to-one function  $f$ .**

25)  $f(x) = \frac{x - 10}{x + 8}$

25) \_\_\_\_\_

**(4 POINTS) Solve.**

26)  $\log_x 625 = 4$

26) \_\_\_\_\_

**(4 POINTS) Solve the exponential equation.**

27)  $e^{-0.19t} = 0.15$

27) \_\_\_\_\_

**(6 POINTS) Solve the logarithmic equation.**

28)  $\log(3 + x) - \log(x - 5) = \log 5$

28) \_\_\_\_\_

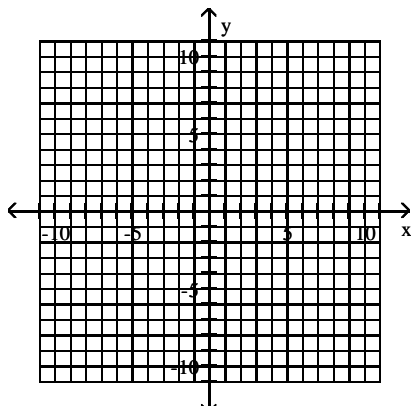
29)  $\log(x + 9) = 1 - \log x$

29) \_\_\_\_\_

**(7 POINTS) Find the center and radius and draw the graph. Label at least 5 points on the graph**

30)  $x^2 + y^2 + 6x + 4y + 9 = 0$

30) \_\_\_\_\_

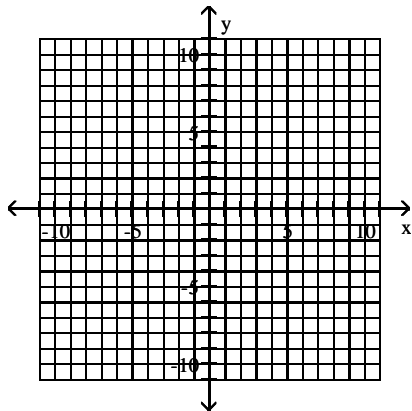




(5 POINTS) Graph the ellipse. Give the points above, below, to the left, and to the right of the center.

$$31) \frac{(x - 4)^2}{9} + \frac{(y - 3)^2}{16} = 1$$

31) \_\_\_\_\_



(8 POINTS) Solve the system of equations.

$$32) \begin{cases} y = 10x - x^2 \\ 2x - y = -15 \end{cases}$$

32) \_\_\_\_\_

$$33) \begin{cases} 3x^2 - 2y^2 = -2 \\ 2x^2 + 2y^2 = 82 \end{cases}$$

33) \_\_\_\_\_

**(8 POINTS) Translate the problem to a system of equations, then solve using substitution or elimination method.**

- 34) A shopkeeper ordered a total of 70 lb of cashews and peanuts. If he ordered 42 less pounds of cashews than peanuts, then how many pounds of peanuts did he order? 34) \_\_\_\_\_

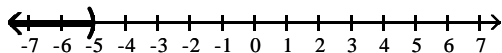
**(6 POINTS) Compute the compound interest.**

- 35) How long will it take for \$500 to grow to \$3200 at an interest rate of 9.8% if the interest is compounded continuously? Round the number of years to the nearest hundredth. 35) \_\_\_\_\_

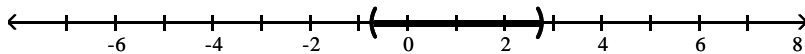
# Answer Key

Testname: M125FINS

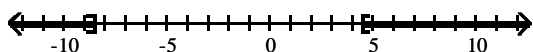
1)  $(-\infty, -5)$



2)  $\left[-\frac{3}{4}, \frac{11}{4}\right]$



3)  $\left(-\infty, -\frac{17}{2}\right] \cup \left[\frac{9}{2}, \infty\right)$

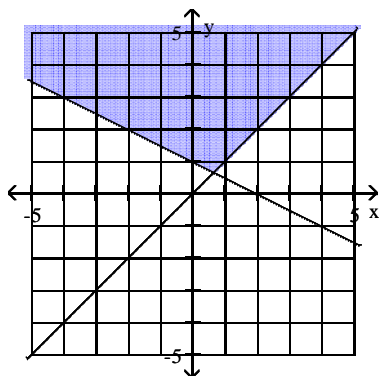


4)  $(-4, 5)$

5)  $(0, -5)$

6)  $(0, -4, 5)$

7)



8)  $38\sqrt{2}$

9)  $12\sqrt{6} + 9\sqrt{15} + 16\sqrt{34} + 12\sqrt{85}$

10)  $\frac{15\sqrt{13}}{13}$

11)  $\frac{1}{41}(\sqrt{42} + 1)$

12)  $60 - 36i$

13)  $\frac{5}{29} + \frac{31}{29}i$

14)  $\frac{1 \pm 3i}{2}$

15)  $\frac{-3 \pm 3\sqrt{5}}{2}$

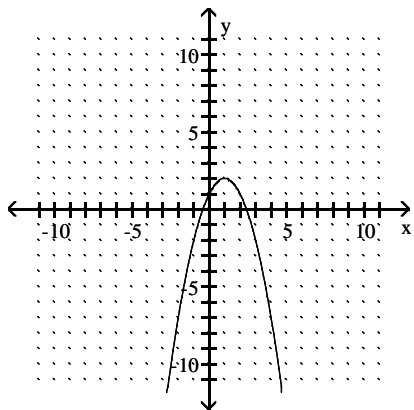
16)  $5 \pm 6i$

17)  $\frac{-7 \pm i\sqrt{15}}{16}$

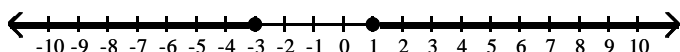
18) 6, 10

Answer Key  
 Testname: M125FINS

- 19) 9
- 20)  $\pm 2, \pm i$
- 21)



22)  $(-\infty, -3] \cup [1, \infty)$

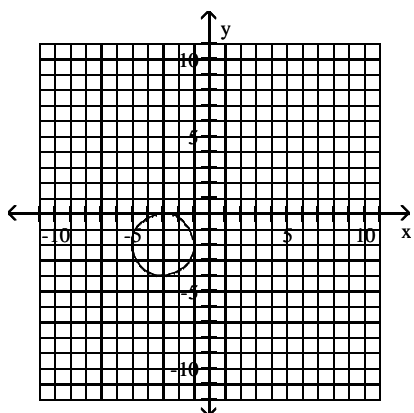


23)  $\left[\frac{17}{6}, \frac{17}{5}\right]$

24)  $(f \circ g)(x) = 2\sqrt{5x + 16}$

25)  $f^{-1}(x) = \frac{-8x - 10}{x - 1}$

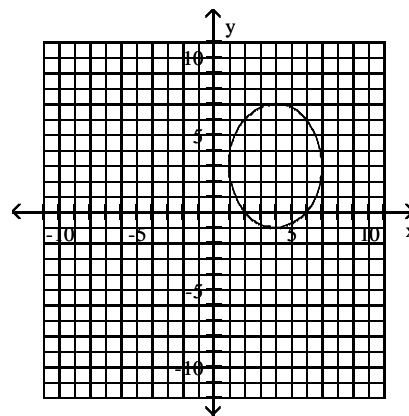
- 26) 5
- 27) 9.9848
- 28) 7
- 29) 1
- 30)



center  $(-3, -2)$ ; radius 2

Answer Key  
 Testname: M125FINS

31)



$(1, 3), (7, 3), (4, 7), (4, -1)$

- 32)  $(5, 25), (3, 21)$
- 33)  $(4, 5), (-4, 5), (4, -5), (-4, -5)$
- 34) 56 lb
- 35) 18.94 yr